

Using R to Keep it Simple: Exploring Structure in Multilevel Datasets

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Point 1: Before starting R have a question you want to answer.

In the United States, the relationship between education and political participation in the cross-section is well known: better educated people tend to be the types that get involved in politics. Extant theories suggest that this relationship exists because (1) people who are better educated have more of the skills they need to do the work of political participation (Verba, Scholzman and Brady, 1995) and (2) people who are better educated are more likely to know other political actors, i.e. they have higher status in the kinds of social networks that matter for political involvement (Nie, Junn and Stehlik-Barry, 1996; Rosenstone and Hansen, 1993; Huckfeldt, 1979).

If we looked at the relationship between education and participation in other countries, would these theories travel? Would education as “civic skills,” such as knowing how to write letters or chair meetings, have the same impact on civic activity in a country where nearly everyone is highly educated as in a country where very few people are literate? Probably not. Would education matter as much in a place where social status is conferred at birth as it does in a place where social status is tied to a college degree? Probably not. These suppositions raise the question about what might be determining who participates across a variety of places, where education plays different roles in society. Answers to this question might tell us something new about the societal bases of political activity, as well as providing new perspectives on 50 years worth of literature based largely on studies of ordinary citizens in the USA.

The question I posed about whether the theories of political participation travel is in essence a question about whether a relationship between variables measured at one level (among ordinary people) depends in some way on variables measured at another level (among countries). This article is written now because we are finally getting data to address such questions directly on a large scale via the Comparative Study of Electoral Systems (CSES Secretariat), the World Values Survey (Inglehart et al.), the African/Euro/Latino Barometers (The Afrobarometer Network; European Commission; Lagos and The Latinobarometro Corporation), and others. Also, within the study of domestic politics, more and more researchers are gathering data on attributes of both citizens and the electoral districts or other geographies in which they are embedded. In fact, I wager a bottle of Kwak (a Belgian beer) that the number of articles in political science journals concerned with quantitative analysis of datasets with more than one type of unit of analysis has more than doubled in the last 10 years.

A dataset used to answer questions about people nested within geographies tends to have fewer countries/districts/states (i.e., macro-level units) than individuals/towns/firms (i.e., micro-level units). And analyses based on such datasets tend to focus on how differences across macro-units somehow condition or influence the differences within macro-units.¹ To address the question I posed earlier, I use the World Values Surveys and European Values Surveys 1999-2001 combined file (ICPSR # 3975) for the micro-level variables of educational attainment and political participation. For macro-level data I use information from

¹I am leaving time out of this article to keep it simple.

the OECD in 2003 on the percent of the population aged 25 to 64 who have a college degree. Since I am using these data to illustrate a series of techniques rather than to answer exhaustively an analytic question, I selected 25 countries, mostly from Europe, to show high variance in the country-level educational context. The political participation variable counts the number out of five possible activities done by individuals in the surveys.² The final dataset contains 36,174 people across 25 countries, and the amount of information available within countries ranges from 968 people in Iceland to 4607 people in Turkey (50% of the countries have between 1015 and 1522 cases). Here is what the data set looks like for a few survey respondents:³

```
> fulldat[c(1:5, 36169:36174), c("country", "id", "partic", "educ2",
+   "pctcollege")]
```

	country	id	partic	educ2	pctcollege
1	Austria	26875	0	1	7
2	Austria	26876	0	1	7
3	Austria	26877	1	3	7
4	Austria	26878	0	1	7
5	Austria	26879	0	1	7
36169	United States	114302	NA	3	28
36170	United States	114303	0	3	28
36171	United States	114304	1	2	28
36172	United States	114305	0	4	28
36173	United States	114306	1	5	28
36174	United States	114307	0	3	28

This excerpt of the full dataset shows six columns: the row numbers that are automatically generated by R; the label of the country in which the survey took place (**country**); respondent identification number (**id**); number of participatory acts reported by that person (**partic**); the educational attainment of that person (**educ2**); and the percent of adults aged 25-64 who have a college degree in that country (**pctcollege**). Notice that **pctcollege** and **country** are the same for every respondent within a given country. This is a very common structure for multilevel datasets.

Point 2: Plot First, Model Later

Just to be concrete, say I wonder (1) whether the relationship between participation and education differs across countries, and (2) if it does differ, whether the difference could have something to do with inequality in educational attainment within countries. The motivation behind the second question is to shed some light on the theory that, in addition to teaching people civic skills, education matters for participation because it allocates social status in a society. In a place where everyone has a college degree, we would not expect education to distinguish participators from non-participators.

The techniques I propose here are meant as a prelude to any statistical procedures that might be suggested to estimate coefficients and related stars (err, standard errors). These

²The activities are signing a petition, joining in boycotts, attending lawful demonstrations, joining unofficial strikes, or occupying buildings.

³The dataset used to produce this article is available for download at <http://www.umich.edu/~jwbowers/papers.html>. The article itself was produced using Sweave (<http://www.ci.tuwien.ac.at/~leisch/Sweave/FAQ.html>). Sweave is a system for embedding R code and output within a L^AT_EX document. That is, this article was produced from one single file that contained both text in L^AT_EX format, and chunks of R code. Sweave ensures that R code is printed out with “>” to mark the beginning of a command line and a “+” to indicate that a command line has continued. In the actual R code I typed the commands without “>” or “+” characters. See my file for an example of how this was done. An excellent introduction to R syntax can be downloaded from <http://cran.r-project.org/manuals.html>.

techniques will help you decide which kind of analysis you will eventually want to conduct and which modeling assumptions are more or less tenable. The idea is simple: run a regression for each country and then plot the coefficients.⁴ The idea of running 25 different regressions, one per country, and making at least 25 different plots is enough to make most peoples' eyes glaze over. This is where R (R Development Core Team, 2004) makes life much easier. The following 2 lines of R code run 25 regressions, collect the 25 regression objects in a list named `theregs`, and add names to the list object for the appropriate countries (naming things turns out to make life a bit easier down the road).⁵

```
> theregs <- lapply(unique(fulldat$country), function(x) {
+   lm(partic ~ educ2, data = fulldat[fulldat$country == x, ])
+ })
> names(theregs) <- unique(fulldat$country)
```

To make things easier for plotting, I collect the coefficients from the regressions into a matrix called `coefmat` and the standard errors into a matrix called `semat`. Then, I combine coefficients, standard errors, and country-level information into a data frame that I can use for plotting. I also make a new macro-level variable called `educgroupsQ` which breaks the country-level educational context variable into three groups — low, middle, and high. Finally, I print the first three rows of the `coefmat` matrix.

```
> coefmat <- matrix(unlist(lapply(theregs, coef)), ncol = 2, byrow = TRUE,
+   dimnames = list(names(theregs), c("Intercept", "Educ")))
> semat <- matrix(unlist(lapply(theregs, function(x) summary(x)$coef[,
+   "Std. Error"])), ncol = 2, byrow = TRUE, dimnames = list(names(theregs),
+   c("SEIntercept", "SEEduc")))
> coefsdf <- data.frame(coefmat, semat)
> coefsdf$country <- factor(row.names(coefsdf))
> coefdf <- merge(coefsdf, themacrodat, by = "country")
> row.names(coefdf) <- as.character(coefdf$country)
> coefdf$educgroupsQ <- cut(coefdf$pctcollege, quantile(coefdf$pctcollege,
+   p = c(0, 0.25, 0.75, 1)), include.lowest = TRUE)
> print(coefdf[1:3, ], 4)
```

	country	Intercept	Educ	SEIntercept	SEEduc	pctcollege
Austria	Austria	0.4031417	0.2028249	0.04234842	0.01665069	7
Belgium	Belgium	0.7135492	0.2241669	0.06801391	0.02143756	13
Brazil	Brazil	0.3608015	0.2346767	0.05695525	0.02247269	8
	educgroupsQ					
Austria		[7,11]				
Belgium		(11,19]				
Brazil		[7,11]				

Figure 1 shows the scatter plots of participation by education within nine of the 25 countries, jittered to show the density of the points at each coordinate. The panels are plotted in order

⁴This idea is not new to me or really that new in general. For great conversations about this, though, I should thank Chris Achen, Steve Heeringa, Dave Howell, Karen Long Justo, and Phil Shively and the Comparative Study of Electoral Systems for hosting us all for a day. Michael Herron and Cara Wong provided important comments and criticisms on this article. And Jusko (2004) presents some other ways to plot within country coefficients in the context of presenting a meta-analysis style approach to estimating the effects of country-level characteristics on individual-level outcomes.

⁵This is another place where I'm playing a bit fast and loose. The educational attainment scale is coded 0=incomplete primary education, 1=completed primary education, 2=incomplete secondary education, 3=completed secondary, 4=incomplete university level, and 5=completed university level. This is not an interval level measure, but I am treating it as such for the purpose of illustration here.

of the percent of their population aged 25-64 who have a college degree (with the United States having the highest proportion and Austria the lowest). The plots for the countries in the lowest education group are colored black, the middle group is colored dark gray, and the highest group is colored light gray. Each panel contains a regression line (the straight one) and a line connecting the mean participation levels at each level of educational attainment (the not straight one). I included the line of means as a check for non-linear relationships. The percent attending college in the country is also printed in each panel.

```
> themeans <- tapply(fulldat$partic, list(country = fulldat$country,
+     educ2 = fulldat$educ2), function(x) mean(x, na.rm = TRUE))
> somecountries <- c("Austria", "Brazil", "Chile", "Spain", "Sweden",
+     "Japan", "Denmark", "Norway", "United States")
> smallcoefdf <- coefdf[coefdf$country %in% somecountries, ]
> countriesInOrder <- as.character(smallcoefdf$country[order(smallcoefdf$pctcollege)])
> thecols <- gray(c(0.1, 0.5, 0.8))
> quartz()
```

```

> par(mfrow = c(3, 3), pty = "s", mar = c(1, 1, 2, 1), mgp = c(1.5,
+   0.5, 0), oma = c(3, 3, 0, 0))
> ps.options(pointsize = 12)
> for (i in countriesInOrder) {
+   plot(jitter(fulldat[fulldat$country == i, "educ2"]), jitter(fulldat[fulldat$country ==
+     i, "partic"]), type = "p", col = thecols[unclass(coefdf[i,
+       "educgroupsQ"])]), xlab = "", ylab = "", xlim = range(fulldat$educ2,
+     na.rm = TRUE), ylim = range(fulldat$partic, na.rm = TRUE),
+     cex = 1)
+   title(main = i, cex = 1)
+   text(0, 4.5, paste("% College=", coefdf[i, "pctcollege"],
+     sep = ""), pos = 4, font = 2, cex = 1)
+   abline(coef(theregs[[i]]))
+   lines(0:5, themeans[i, ])
+ }
> mtext(side = 1, "Educational Attainment", outer = TRUE, line = 1)
> mtext(side = 2, "Number of Participatory Acts", outer = TRUE,
+   line = 1)

```

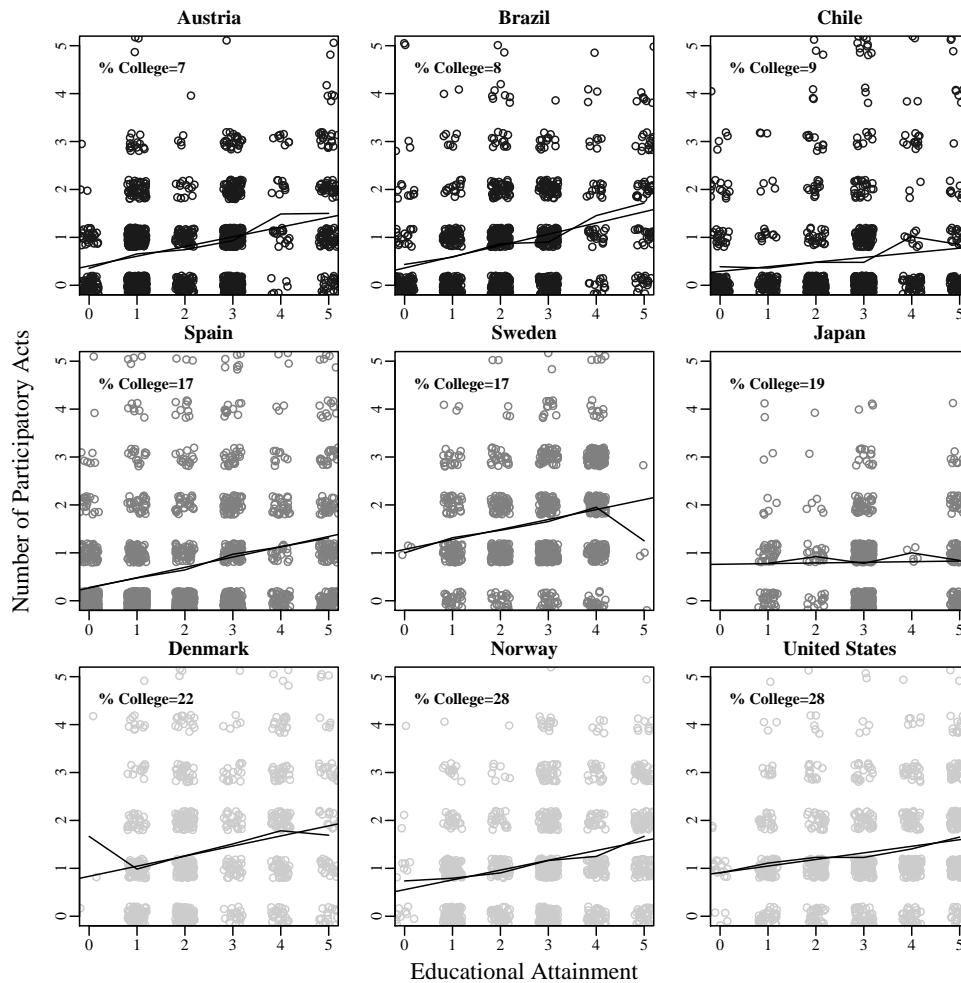


Figure 1: Within Country Regressions and Means Sorted by Proportion of the Population with a College Degree

The Lattice graphics (Sarkar, 2004) sub-system within R provides a quicker and more elegant way to produce a similar plot.⁶ Figure 2 shows this plot. It is my experience that lattice graphics (functions like `xyplot()`) are usually less flexible than the lower level plotting commands (e.g., functions like `plot()`). However, they can produce reasonable plots more quickly than the lower level commands — for example, in this next example, the regressions are run and plotted with the `panel.lmline()` function. This means that if our plotting were to stop here, we wouldn't have needed to create our dataset of coefficients and standard errors.

```
> library(lattice)
> fulldat$countryEducOrder <- factor(fulldat$country, levels = levels(fulldat$country)[order(coef
+   ordered = TRUE)
> latticeplot <- xyplot(partic ~ educ2 | countryEducOrder, data = fulldat,
+   cex = 0.7, subset = fulldat$country %in% somecountries, xlab = "Education Level",
+   ylab = "Number of Participatory Acts", panel = function(x,
+     y, ...) {
+       panel.xyplot(jitter(x), jitter(y), col = "gray", ...)
+       panel.lmline(x, y, ..)
+       themeans <- tapply(y, x, function(x) mean(x, na.rm = TRUE))
+       llines(as.numeric(dimnames(themeans)[[1]]), themeans,
+         col = "black")
+     })
```

⁶The manual for Lattice graphics explains: “Trellis Graphics is a framework for data visualization developed at the Bell Labs by Rick Becker, Bill Cleveland et al, extending ideas presented in Bill Cleveland’s 1993 book *Visualizing Data* (Cleveland, 1993). Lattice is best thought of as an implementation of Trellis Graphics for R.” (Sarkar, 2004)

```
> print(latticeplot)
```

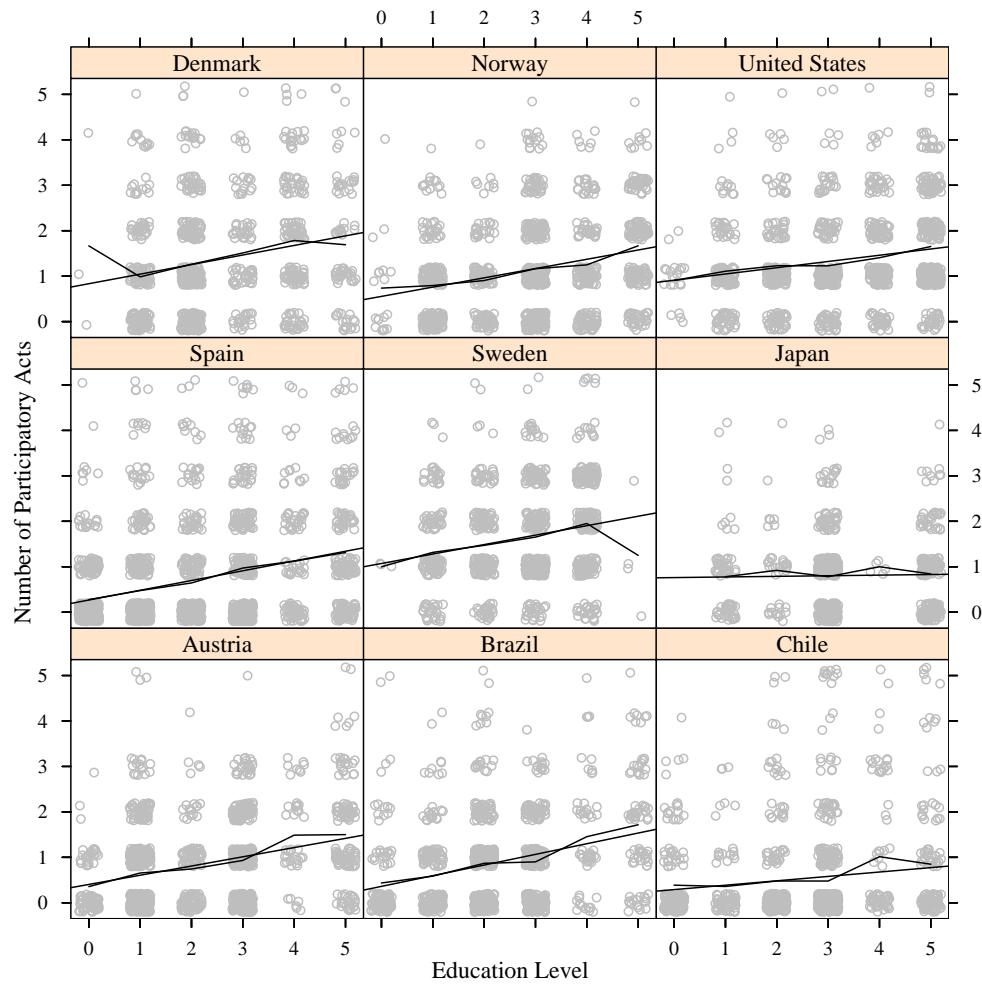


Figure 2: Within Country Regressions and Means Sorted by Proportion of the Population with a College Degree: Lattice Graphics

If we do not have a continuous macro-level variable, we might want to plot these regression lines groups together — with the mean line overlaid. Figure 3 shows the within country regression lines (bounded at the limits of the education variable) plotted together within groups defined by the percent of the population receiving a college degree.⁷

```
> thefits <- lapply(theregs, function(x) {
+   thenewdata <- range(x$model$educ2)
+   data.frame(cbind(x = thenewdata, y = predict(x, newdata = data.frame(educ2 = thenewdata))))
+ })
```

⁷The thick mean lines do not take into account the amount of information that went into the estimation of the different lines. I leave the creation of a weighted average line as an exercise.

```

> ps.options(width = 7, height = 3, family = "Times", pointsize = 10)
> par(mfrow = c(1, 3), pty = "s", mar = c(1, 1, 2, 1), mgp = c(1.5,
+   0.5, 0), oma = c(2, 2, 0, 0))
> for (i in levels(coefdf$educgroupsQ)) {
+   plot(range(fulldat$educ2, na.rm = TRUE), range(unlist(lapply(thefits,
+     function(x) range(x$y))))), type = "n", xlab = "", ylab = "",
+     main = paste("Range % College=", i))
+   lapply(thefits[coefdf$educgroupsQ == i], function(x) {
+     lines(x$x, x$y, col = gray(0.5))
+   })
+   tempdf <- data.frame(thefits[coefdf$educgroupsQ == i])
+   meanpartic <- rowMeans(tempdf[, grep("y$", names(tempdf))])
+   lines(c(0, 5), meanpartic, lwd = 3)
+ }
> mtext(side = 1, "Educational Attainment", outer = TRUE)
> mtext(side = 2, "Number of Acts", outer = TRUE, line = 1)

```

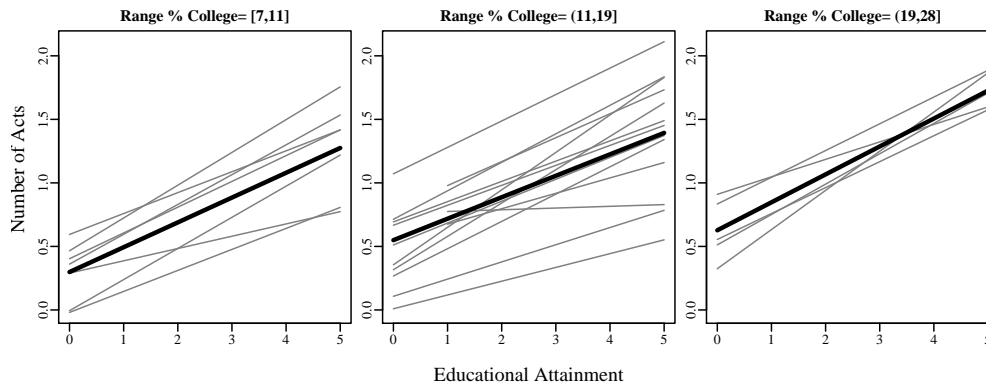


Figure 3: The Relationship between Educational Attainment and Political Participation by Educational Context of Countries

Now let us look at the change in the individual level effects of education on participation by the country-level educational attainment level more systematically. Since we have collected the coefficients and standard errors in a dataset, we can look at how the relationship between education and participation varies across countries based on the educational inequality at the country-level, by treating these coefficients as data and the standard errors as weights.

Figure 4 shows the coefficients from within country regressions plotted against the percent of college educated within a country. The line segments through each point show the ± 2 standard error range around each point — to alert us to the amount of information used in the calculation of that estimate. The straight lines in each panel show the regression of the coefficients on country level education. The wiggly lines are a non-parametric regression. And, points that fall far from the regression line are labeled. Both the linear regression and the non-parametric smoother are weighted by the standard errors of the within country regressions.

```

> EducOnPctCollW <- lm(Educ ~ pctcollege, data = coefdf, weights = 1/SEEduc)
> interceptOnPctCollW <- lm(Intercept ~ pctcollege, data = coefdf,
+   weights = 1/SEIntercept)
> ps.options(width = 7, height = 4, family = "Times", pointsize = 10)
> attach(coefdf)
> par(mfrow = c(1, 2), pty = "s", mar = c(2, 3, 2, 1), mgp = c(1.5,
+   0.5, 0), oma = c(2, 0, 0, 0))
> plot(pctcollege, Educ, type = "p", ylim = range(Educ - 2 * SEEduc,
+   Educ + 2 * SEEduc), main = "Slopes", xlab = "", ylab = "Effect on Participation")
> segments(pctcollege, Educ - 2 * SEEduc, pctcollege, Educ + 2 *
+   SEEduc)
> abline(EducOnPctCollW)
> plot(locfit(Educ ~ pctcollege, data = coefdf, weights = 1/SEEduc,
+   alpha = 1/2), add = TRUE)
> weirdpoints <- abs(resid(EducOnPctCollW)) > quantile(abs(resid(EducOnPctCollW)),
+   p = c(0.85))
> text(pctcollege[weirdpoints], Educ[weirdpoints], as.character(country)[weirdpoints])
> plot(pctcollege, Intercept, type = "p", ylim = range(Intercept -
+   2 * SEIntercept, Intercept + 2 * SEIntercept), main = "Intercepts",
+   xlab = "", ylab = "Mean Participation")
> segments(pctcollege, Intercept - 2 * SEIntercept, pctcollege,
+   Intercept + 2 * SEIntercept)
> abline(interceptOnPctCollW)
> plot(locfit(Intercept ~ pctcollege, data = coefdf, weights = 1/SEIntercept,
+   alpha = 1/2), add = TRUE)
> weirdpoints2 <- abs(resid(interceptOnPctCollW)) > quantile(abs(resid(interceptOnPctCollW)),
+   p = c(0.85))
> text(pctcollege[weirdpoints2], Intercept[weirdpoints2], as.character(country)[weirdpoints2])
> mtext(side = 1, "Percent of Population 25-64 years old with a College Degree",
+   outer = TRUE, line = 0)
> detach(coefdf)

```

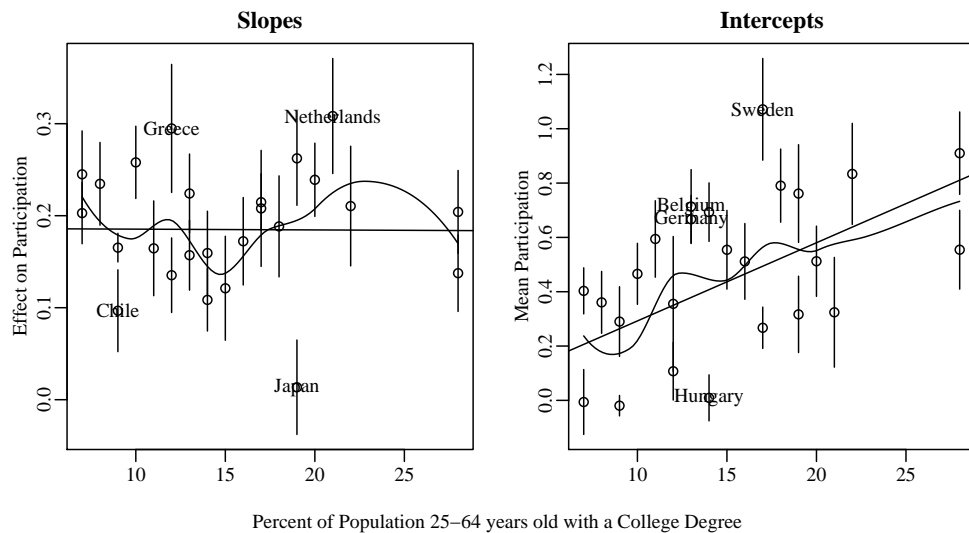


Figure 4: The Relationship Between Education and Participation as a function of the Educational Inequality Of A Country

In the slopes panel, we see that the relationship between an individual’s education and her participation does not depend in any simple linear way on the percent of the population who has a college degree, although there might be some interesting non-linear pattern. Furthermore, we see that Japan is not well characterized by the process that captures the other countries. In the intercepts panel, we see that countries where more people have college degrees tend to have higher participation rates among people with low educational attainment than countries where fewer people have college degrees. In other words, it appears that there is a participation benefit that accrues from living in a place where many people have more education — even for people who do not have high educational levels. Both panels also alert us to the fact that certain countries do not fit the general patterns very well: Japan stands out for having almost no relationship between education and participation, and Sweden and Hungary are places where those with low education appear to participate more and less, respectively, than would be expected given the educational context in those countries.

So far, it is also clear that people who have more education are more likely to get involved in petitions, boycotts, demonstrations, illegal strikes, and sit-ins than people who have less education, *in nearly every country in the dataset*. This result is surprising given my expectations about how political institutions (and social status) ought to be differently related to education in different countries. We have also seen that Japan does not have a pattern like the others. In Japan, in 1999-2001, education did not appear related to participation at all. Notice that if we had skipped this plotting step, we would have estimated some kind of model that produced a coefficient for something like the “average relationship between education and participation” across countries. This coefficient might have had many stars, or not. And, these plots suggest that an average slope might do a good job summarizing these patterns (i.e., the slopes do not look that different across countries). However, the lack of relationship in Japan would have been smoothed over. Since this is an article about how to use R, I will not speculate about what this result means for Japan or for the overall question I posed at the beginning of the article. However, it is worth noting that the plots have taught us something about the phenomenon we care to understand, which would have been hard to pick up in a model specified before looking at the data.

Point 3: Plot to Check Assumptions for Future Modeling

Many popular modeling strategies for multilevel data rely on assumptions about relationships between the slopes and intercepts in within country regressions. For example, most “random effects” or “random coefficients” or “multilevel” models (whether estimated using maximum likelihood or Markov-Chain Monte-Carlo simulation) assume that the slopes and the intercepts can be thought of as drawn from a multivariate normal distribution. How plausible is such an assumption in this case? A priori, it is hard to know. It is plausible that we could have some countries with very strong relationships and others with no relationships — leading to a bimodal distribution of slopes. If this were the case, then the assumptions about normally distributed random coefficients would not be tenable.

The top row of figure 5 shows qqplots where the slopes and intercepts are plotted against what would be expected, were these variables drawn from a normal distribution. The bottom row shows the non-parametric density estimates for the slopes and intercepts. Overall, the slopes and intercepts do look like they could have been drawn from a normal distribution, for a few outlying points.

```

> par(mfrow = c(2, 2), pty = "s", mar = c(3, 2, 2, 1), oma = c(0,
+      0, 0, 0))
> qqnorm(coefdf$Intercept, main = "Are Intercepts Like a Normal Distribution?")
> qqline(coefdf$Intercept)
> qqnorm(coefdf$Educ, main = "Are Slopes Like a Normal Distribution?")
> qqline(coefdf$Educ)
> plot(density(coefdf$Intercept), main = "Density of Intercepts")
> rug(coefdf$Intercept)
> plot(density(coefdf$Educ), main = "Density of Slopes")
> rug(coefdf$Educ)

```

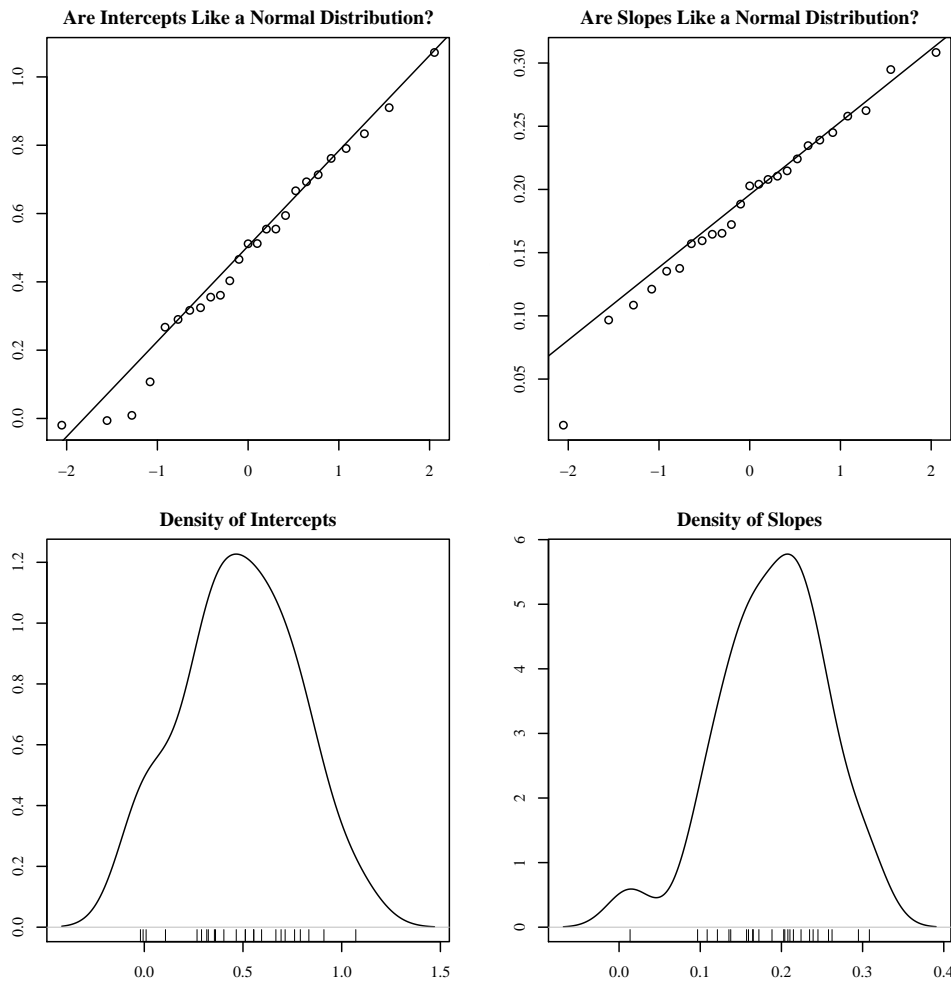


Figure 5: Assessing the Marginal Distributions of the Slopes and Intercepts

What kind of multivariate normal distribution generated these marginally (mostly) normal-looking slopes and intercepts? Are the slopes and intercepts correlated with one another? Figure 6 shows the joint distribution of the slopes and intercepts. The smoothed contour lines representing bivariate density are overlaid on the scatterplot of the slopes and intercepts. We do not see an extremely strong relationship here, and the correlation is $-.13$. This suggests

that countries where people with lower education participate more (i.e., higher intercepts) tend (weakly) to be countries where the relationship between education and participation is weaker than in countries where the least educated participate less.

```
> ps.options(width = 3, height = 3, family = "Times", pointsize = 10)
> par(mfrow = c(1, 1), pty = "s", oma = c(0, 0, 0, 0), mar = c(3,
+   2, 1, 1), mgp = c(1.5, 0.5, 0))
> plot(coefdf$Intercept, coefdf$Educ, pch = 19, col = "black",
+   xlab = "Intercepts", ylab = "Slopes", cex.lab = 1)
> plot(locfit(~Intercept * Educ, data = coefdf, alpha = 3/4, scale = T,
+   kern = "rect", deg = 2, family = "dens"), add = TRUE, col = gray(0.5),
+   drawlabels = TRUE)
> text(coefdf$Intercept[coefdf$country %in% c("Japan", "Sweden")],
+   coefdf$Educ[coefdf$country %in% c("Japan", "Sweden")], c("Japan",
+   "Sweden"), pos = 2)
```

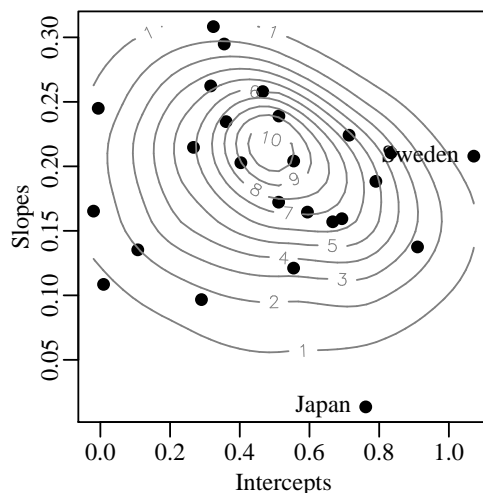


Figure 6: Assessing the Joint Distribution of Slopes and Intercepts

Pretend that these plots were done on a dataset with all of the countries in the World Values Survey, and that within country models included appropriate controls for variables that might be confounding the relationship between education and participation. And, pretend that I had multiple measures of the educational inequality within these countries. If I saw results like those shown here, I would have a story to tell about the expectations that were generated from the previous theories: The theories appear to travel well although educational inequalities in participation appear to be slightly ameliorated within countries where more of the population is better educated. I would also have new questions to spur further research — what is going on with Japan and Sweden? Finally, I would be set up to make reasoned choices about the next steps I might take if I wanted to estimate, say, a single coefficient representing how the relationship between education and participation changes on average across countries. Although running and displaying 25 regressions (or 100) might be a daunting task in other statistical analysis environments, I hope that I've shown (1) how R can make the tasks of getting to know this kind of data easy. and (2) how an interesting substantive story can be told simply and persuasively without an asterisk in sight.

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